

# Residual Stress Analysis by X-Ray Diffraction

- or -

**Those Propeller Stresses Had Better Be  
Compressive !!!**

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# Acknowledgements

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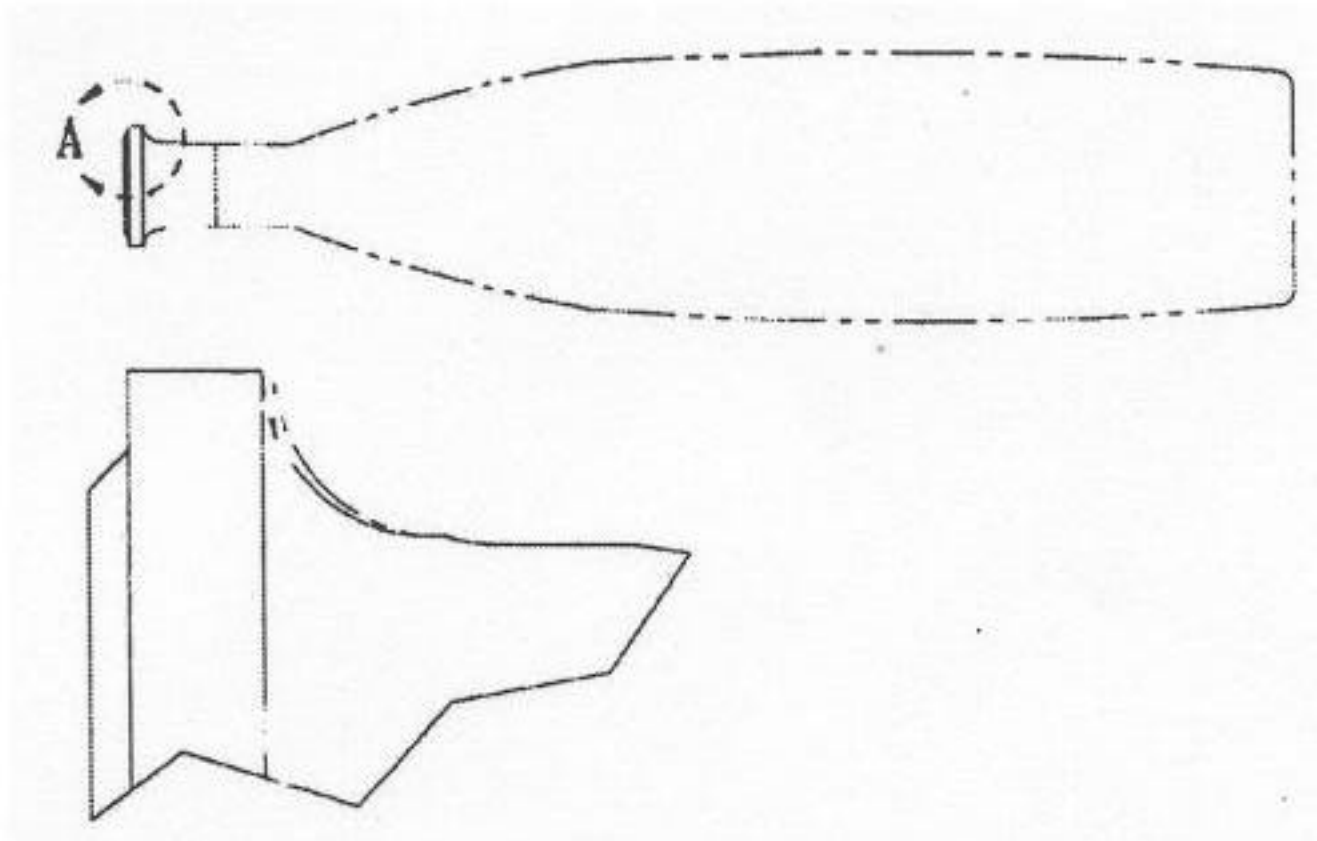
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## Outline

- I. Propeller blades and stresses.
  - II. Why do we need compressive stresses?
  - III. How do we put compressive stresses in propellers?
  - IV. How can we tell what the stresses are?
  - V. Results from the real world
  - VI. Conclusions
-

# Propeller Blades and Stresses

Blade retention feature



## Why Do We Need Compressive Stresses?

- Propeller assembly is a highly energetic rotating assembly
  - Blades operate under severe load conditions
  - Dominant bending loads are imposed at the inboard retention feature
  - Airplanes and helicopters are merely fatigue machines that operate above ground (hopefully!)
  - Compressive stresses extend fatigue life
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# How Do We Put Compressive Stresses in Propellers?

- Plastically deform (move material in) the critical stress areas of a propeller
  - Common methods of imparting compressive stresses:
    - Shot peening
    - Compression rolling
  - Both methods put a compressive stress at the surface and a more compressive stress beneath the surface
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## How Can We Tell What the Stresses Are?

- Strain gage blind hole drilling
  - X-ray diffraction
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# X-Ray Diffraction Residual Stress Measurement

*Definition* - A technique that combines physics, mechanics and alchemy to help one determine the useful life of a part.

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## Loading Versus Residual Stress

- *Loading Stress* - results from applied load: weight, torsion, bending, pressure, pushing, pulling etc.
  - *Residual Stresses* - stresses that remain in the material after all external loads are removed. They result from differential cooling rates (Welding, Heat Treating, etc.) and plastic flow (Shot Peening, Cold Working, etc.).
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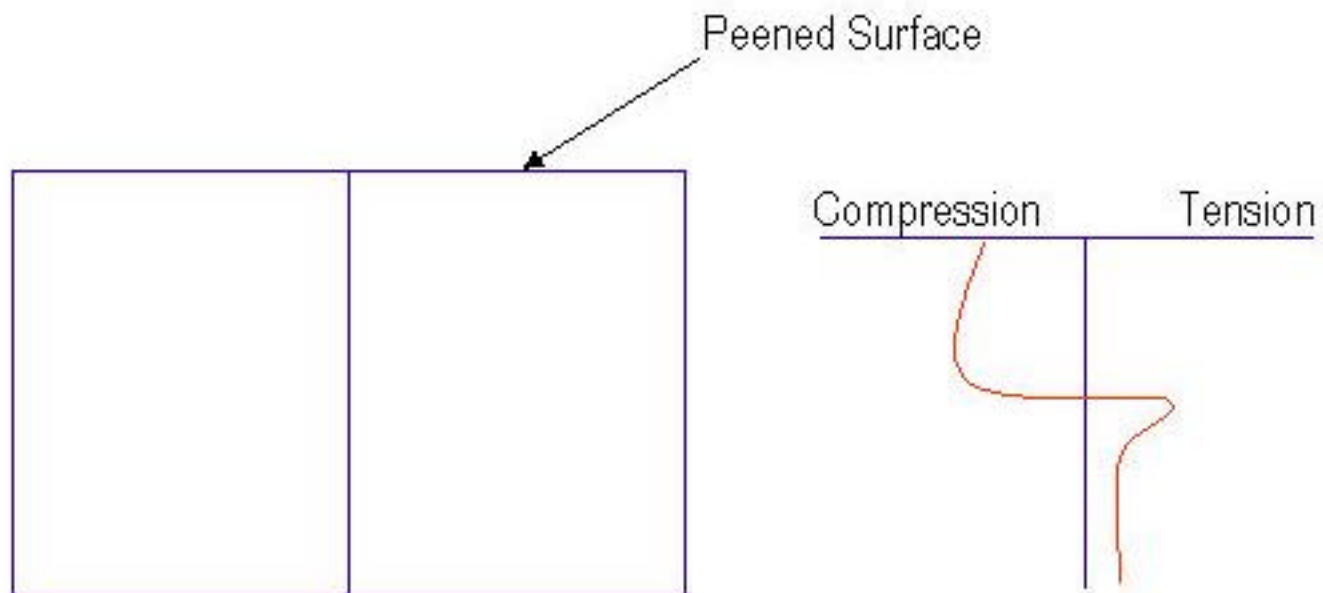
## Origin of Residual Stress

- Introduction by mechanical, thermal, and/or chemical processes that result in a permanent, nonuniform change in shape or volume.
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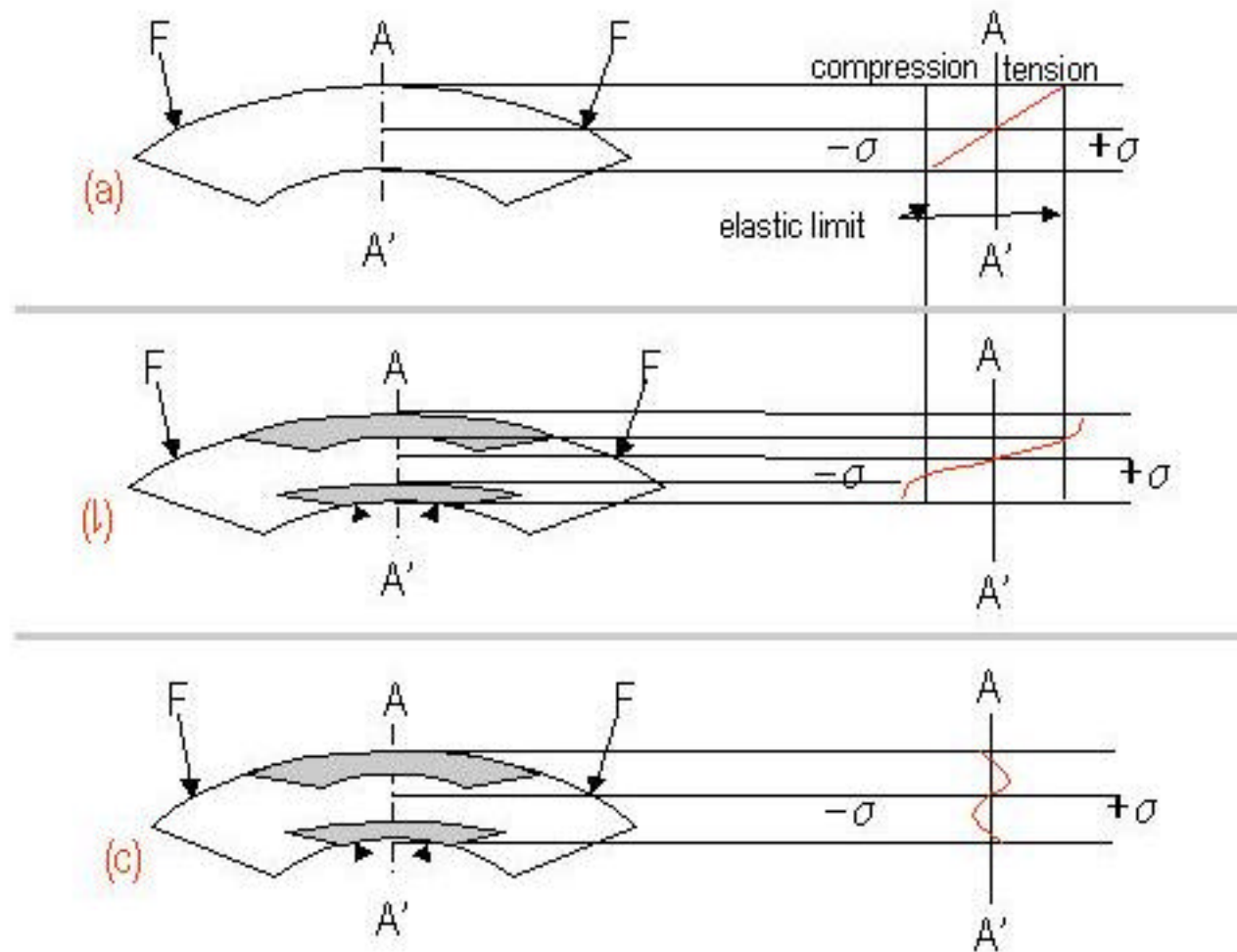
## Mechanical Processes

- Surface Working
    - Shot Peening
    - Surface Rolling
    - Polishing
  - Drawing
  - Rolling
  - Grinding and Machining
  - Assembling
-

# Shot Peening



# Forming



## Benefits of X-Ray Diffraction Residual Stress Analysis

- Can be nondestructive
  - Accurate stress vs. depth with electropolishing
  - Repeatable
  - Fast
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## Benefits (continued)

- Understand and quantify grinding burn to prevent component failure
  - Analyze residual stresses vs. fatigue to aid in useful life estimation
  - Find cause of warping in machined components
  - Analyze heat affected zones of weldments to determine need for stress relief
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## Why Residual Stresses Are Important

- Residual stresses may be harmful or beneficial
  - Tensile residual stresses at surface are normally harmful, sometimes leading to brittle fracture in fatigue
  - Compressive residual stresses at surface normally increase fatigue strength
  - Residual stresses can be controlled in the manufacturing process
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# **INSERT**

## **History of Residual Stress**

### **(X-Ray Diffraction - XRD)**

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## X-Ray Diffraction Stress Measurements

- Measures elastic strains
  - Direct, self calibrating technique
  - Measures long range stresses at a point
  - Can measure complex geometries
  - Can measure phase-by-phase stresses
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# X-Ray Diffraction

## Residual Stress Measurements

- If component is loaded, resultant stress will be the residual plus the applied stress
  - Measurements can be made on most metals and ceramics; samples must be polycrystalline with relatively randomly oriented medium to fine grains
  - Measurements can be made in a few minutes to an hour
-

## X-Ray Diffraction Residual Stress Measurements

- Nondestructive\* surface measurement techniques
- Measures strains, stresses are calculated
- Gives absolute stress value
- Measures residual strain if sample is unloaded

\* depth profiling can be destructive

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# Strain

$$\frac{\Delta l}{l_0} \quad \text{or} \quad \frac{\Delta d}{d_0}$$

# Stress-Strain Relationship

$$\varepsilon_{ii} = \frac{1}{E} \sigma_{ii}$$

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$$\varepsilon_{jj} = \frac{-\nu}{E} \sigma_{ii}$$

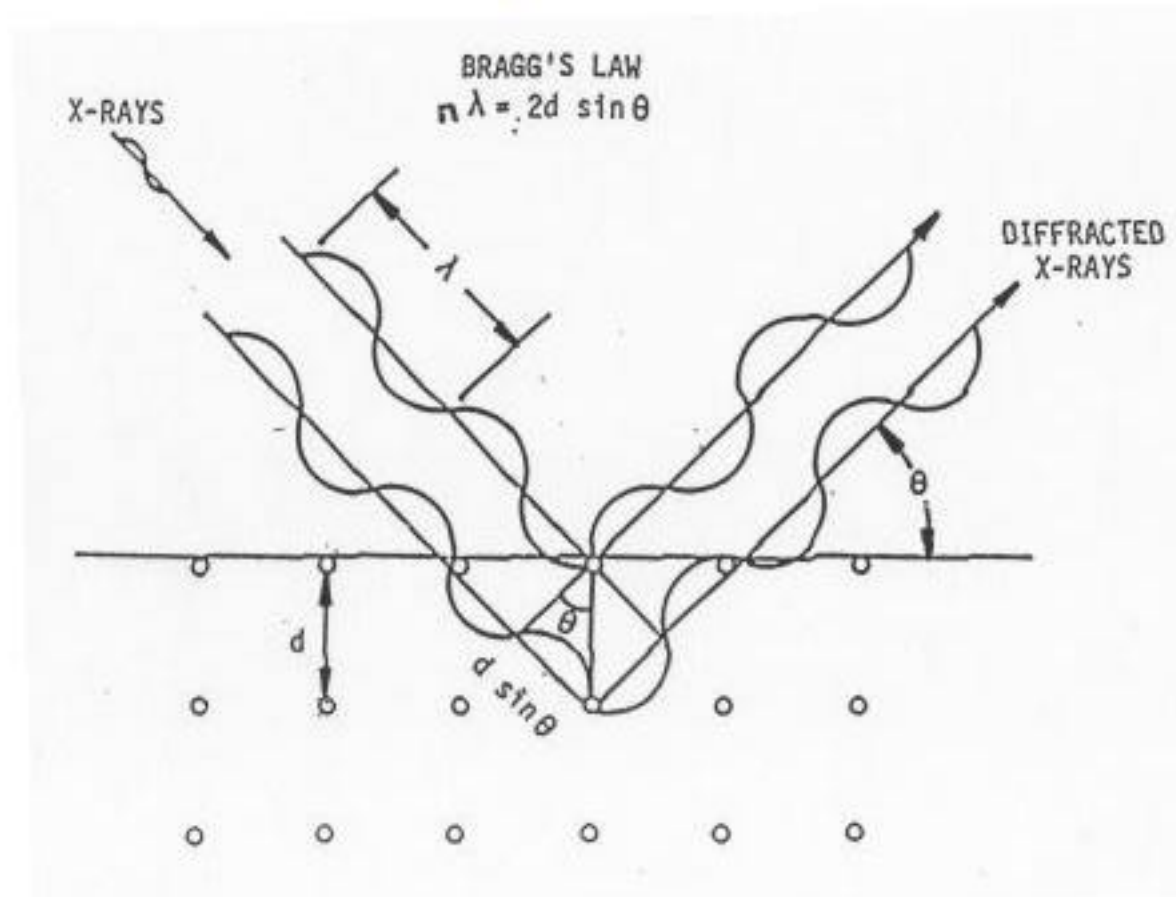
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$$\varepsilon_{ii} = \frac{1}{E} \sigma_{ii} - \frac{\nu}{E} (\sigma_{jj} + \sigma_{kk})$$

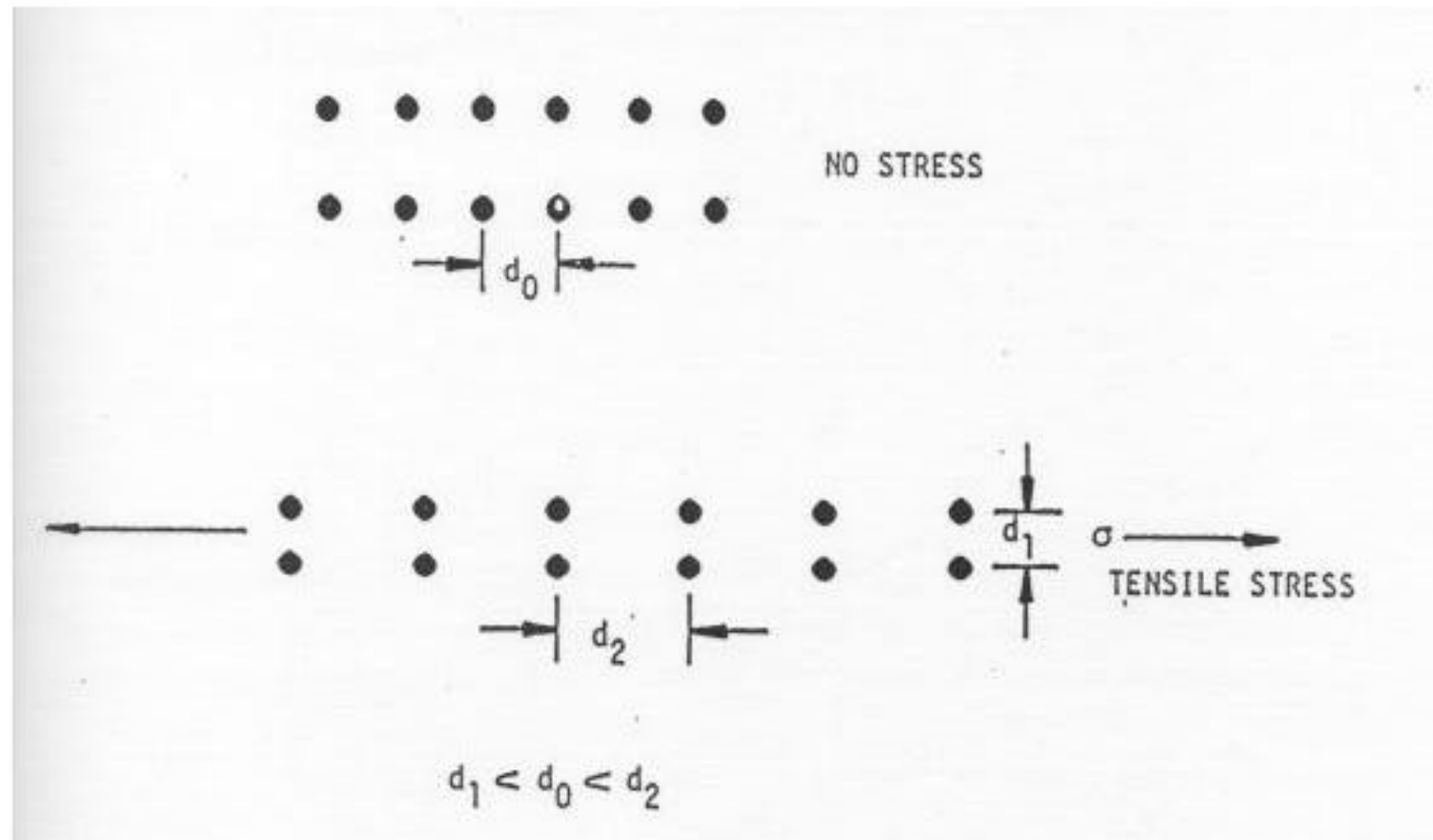
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# Bragg's Law

Used to Measure Crystal Lattice Parameter, "d"

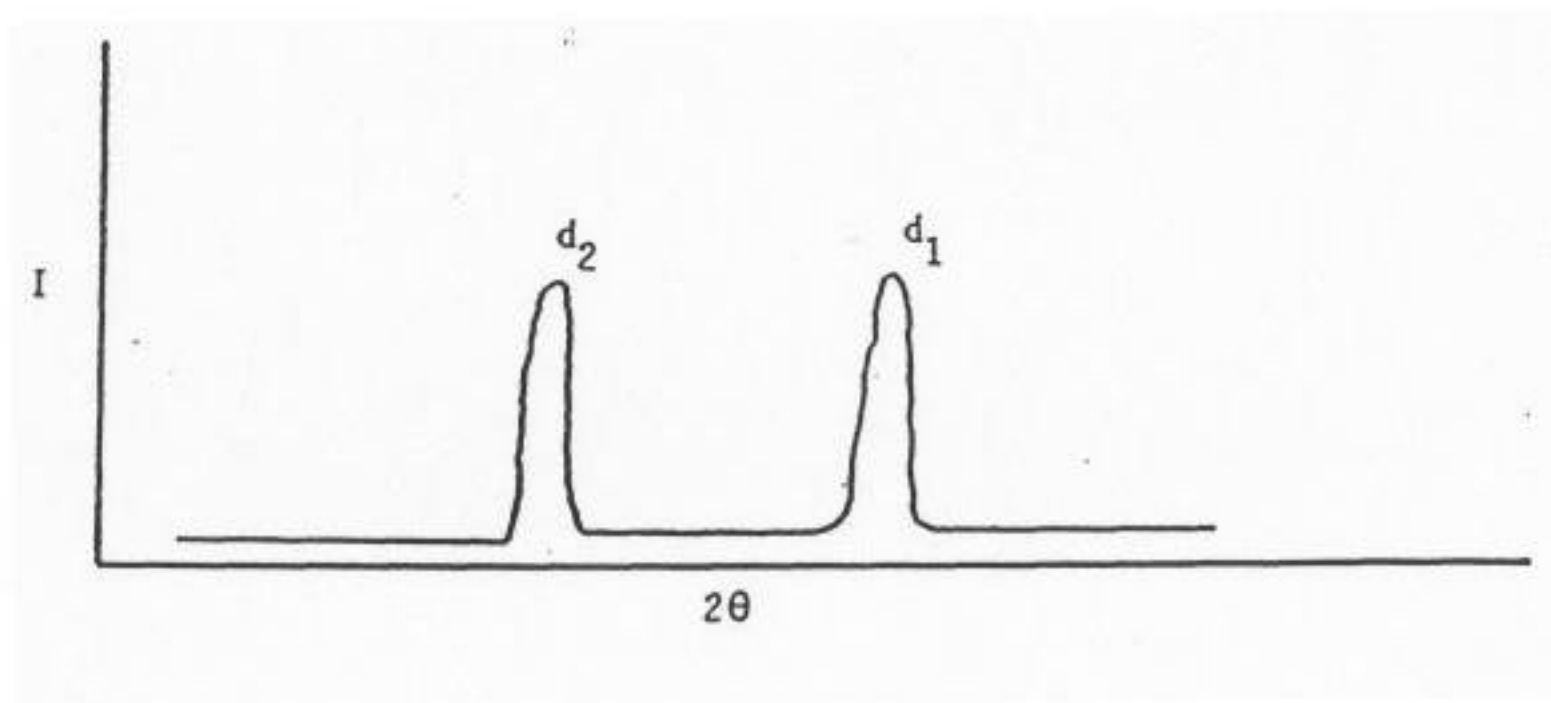


## Effects of Tensile Stress on a Crystal Lattice Structure

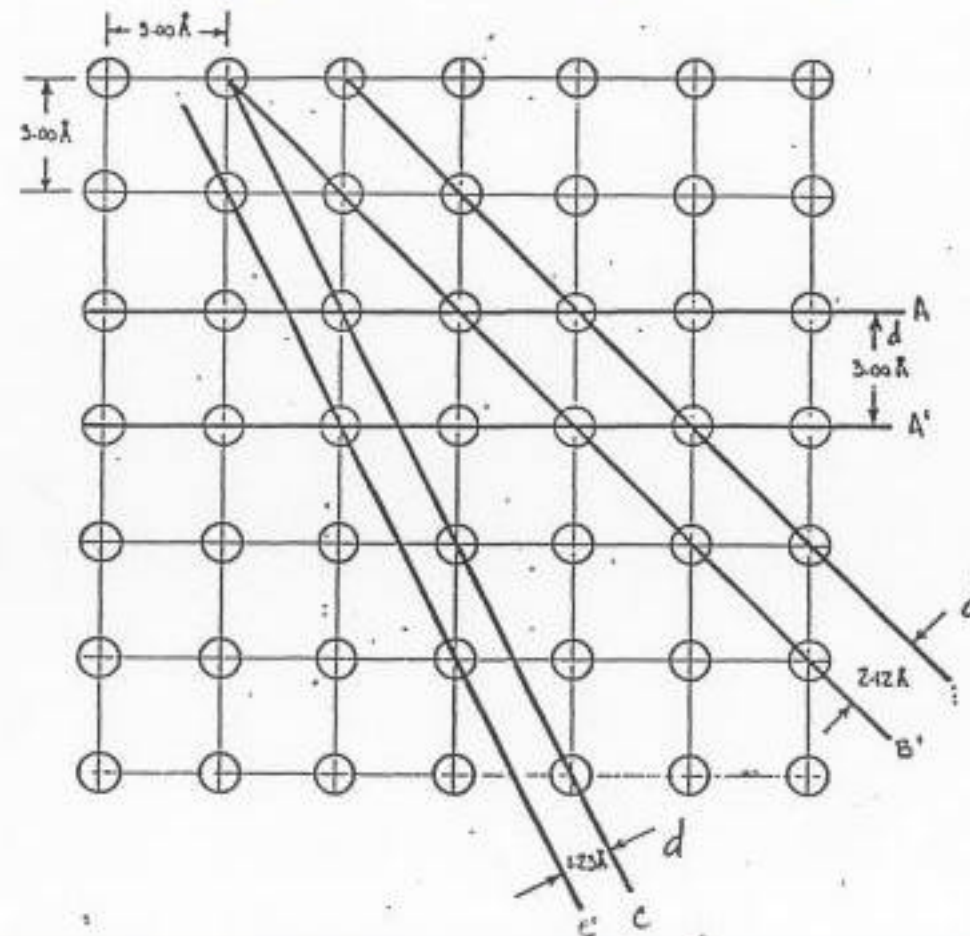




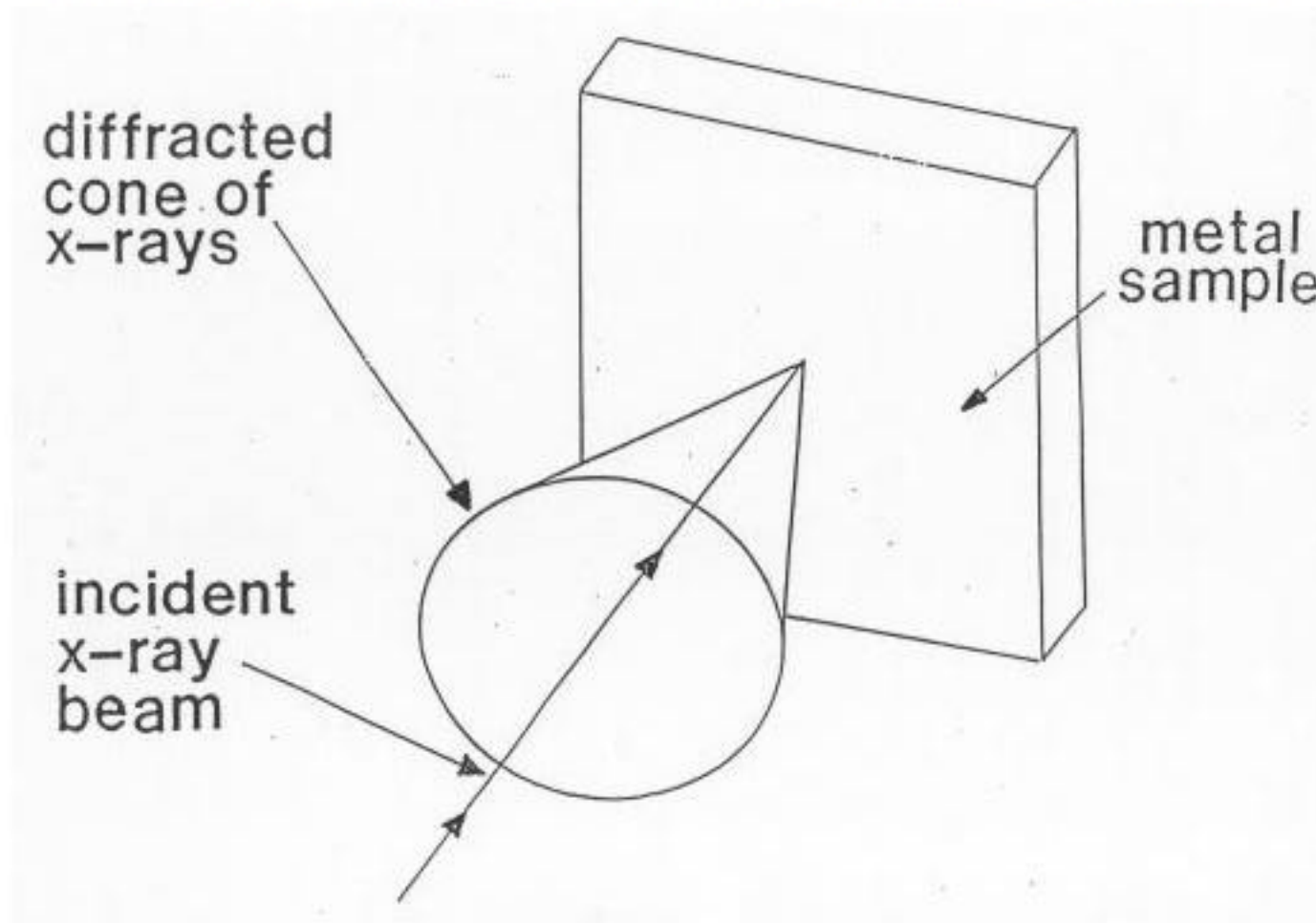
# Diffraction Pattern

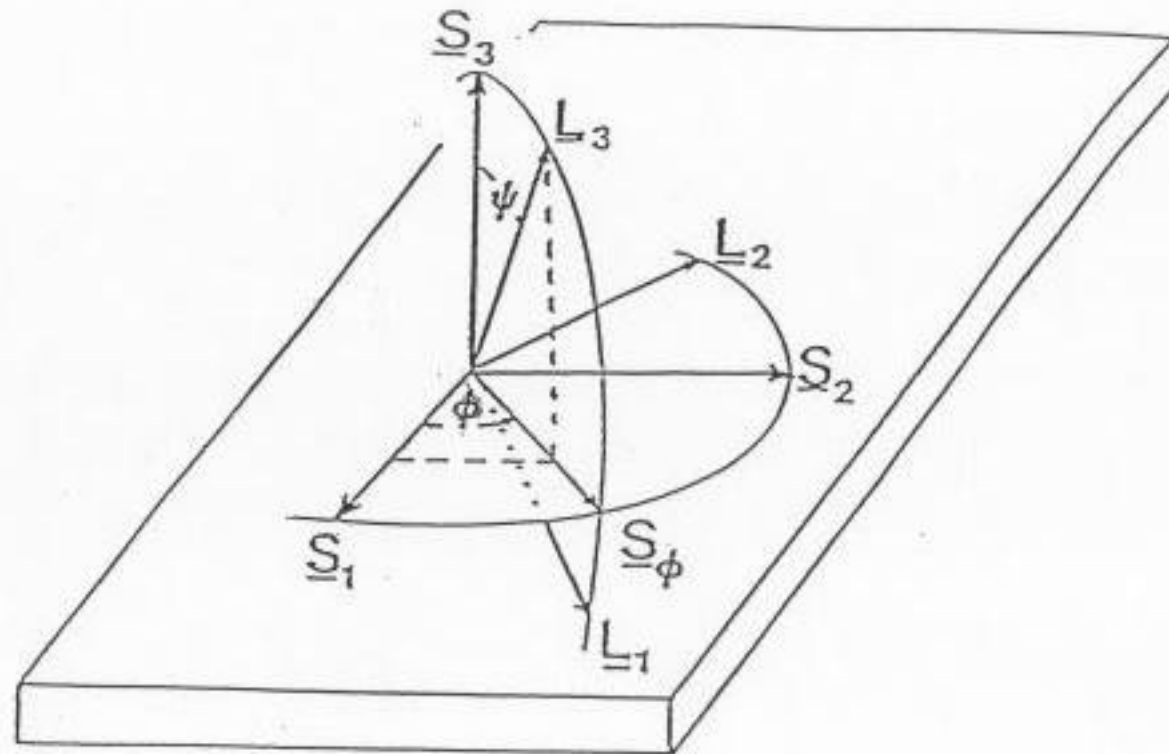


# Interplanar Spacings



# Incident and Diffracted Beams





# Stress-Strain Equation for XRD

$$(\epsilon_{33}) \phi\psi = \frac{d\phi\psi - d_0}{d_0}$$

$$(\epsilon_{33}) \phi\psi = a_{3k} a_{3l} \epsilon_{kl}$$

$$a_{1k} = \begin{vmatrix} \cos\phi \cos\psi & \sin\phi \cos\psi & -\sin\psi \\ -\sin\psi & \cos\phi & 0 \\ \cos\phi \sin\psi & \sin\phi \sin\psi & \cos\psi \end{vmatrix}$$

$$\begin{aligned} (\epsilon_{33}) \phi\psi = \frac{d\phi\psi - d_0}{d_0} &= \epsilon_{11} \cos^2\phi \sin^2\psi + \epsilon_{12} \sin^2\phi \sin^2\psi \\ &+ \epsilon_{22} \sin^2\phi \sin^2\psi + \epsilon_{33} \cos^2\psi \\ &+ \epsilon_{13} \cos^2\phi \sin^2\psi + \epsilon_{23} \sin^2\phi \sin^2\psi \\ &= 1/2 S_2 [\sigma_{11} \cos^2\phi + \sigma_{12} \sin^2\phi \sin^2\psi + \sigma_{22} \sin^2\phi] \sin^2\psi \\ &+ 1/2 S_2 \sigma_{33} \cos^2\psi + S_1 [\sigma_{11} + \sigma_{22} + \sigma_{33}] \\ &+ 1/2 S_2 [\sigma_{13} \cos\phi + \sigma_{23} \sin\phi] \sin^2\psi \end{aligned}$$

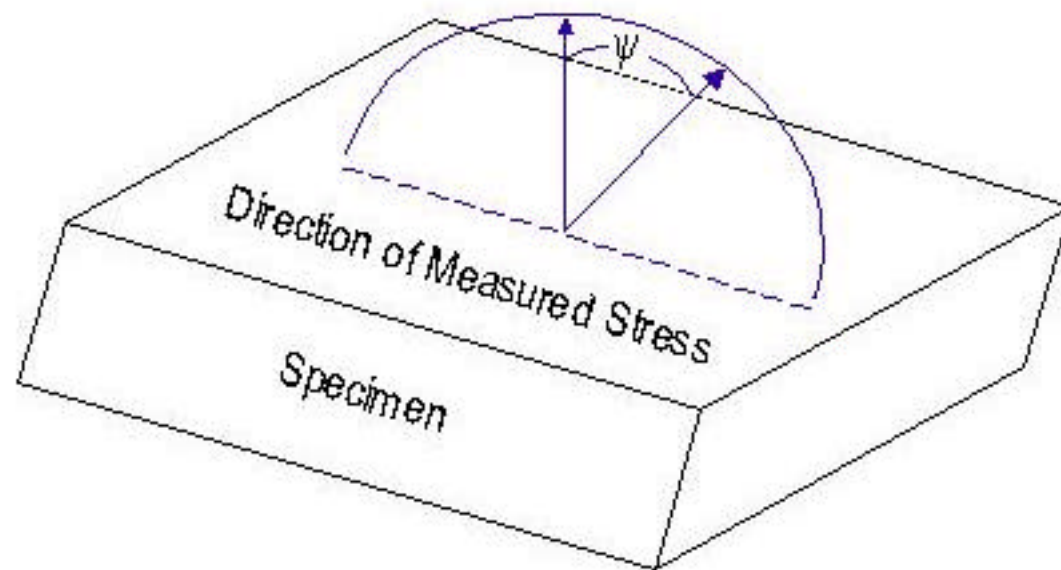
Assuming  $\sigma_{33} = \sigma_{13} = \sigma_{23} = 0$

$$\frac{d\phi\psi - d_0}{d_0} = 1/2 S_2 [\sigma_{11} \cos^2\phi + \sigma_{12} \sin^2\phi + \sigma_{22} \sin^2\phi] \sin^2\psi + S_1 [\sigma_{11} + \sigma_{22}]$$

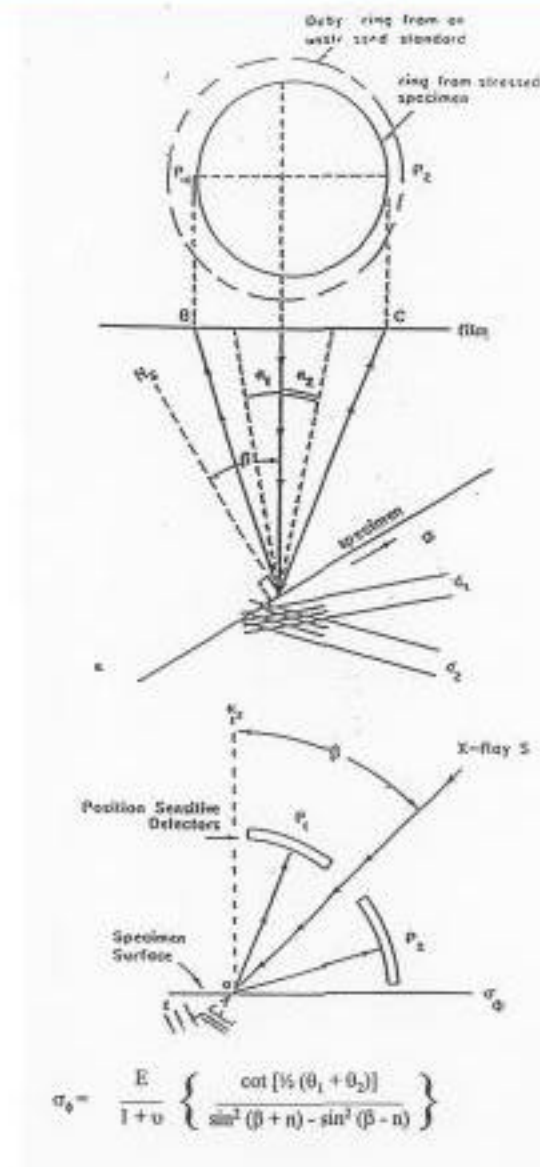
$$\frac{d\phi, \psi = 0 - d_0}{d_0} = S_1 [\sigma_{11} + \sigma_{22}]$$

$$\frac{d_{\phi, \psi} - d_0}{d_0} - \frac{d_{\phi, \psi = 0} - d_0}{d_0} = \frac{d_{\phi, \psi} - d_{\phi, \psi = 0}}{d_0} = 1/2 S_2 \sigma_{\phi} \sin^2\psi$$

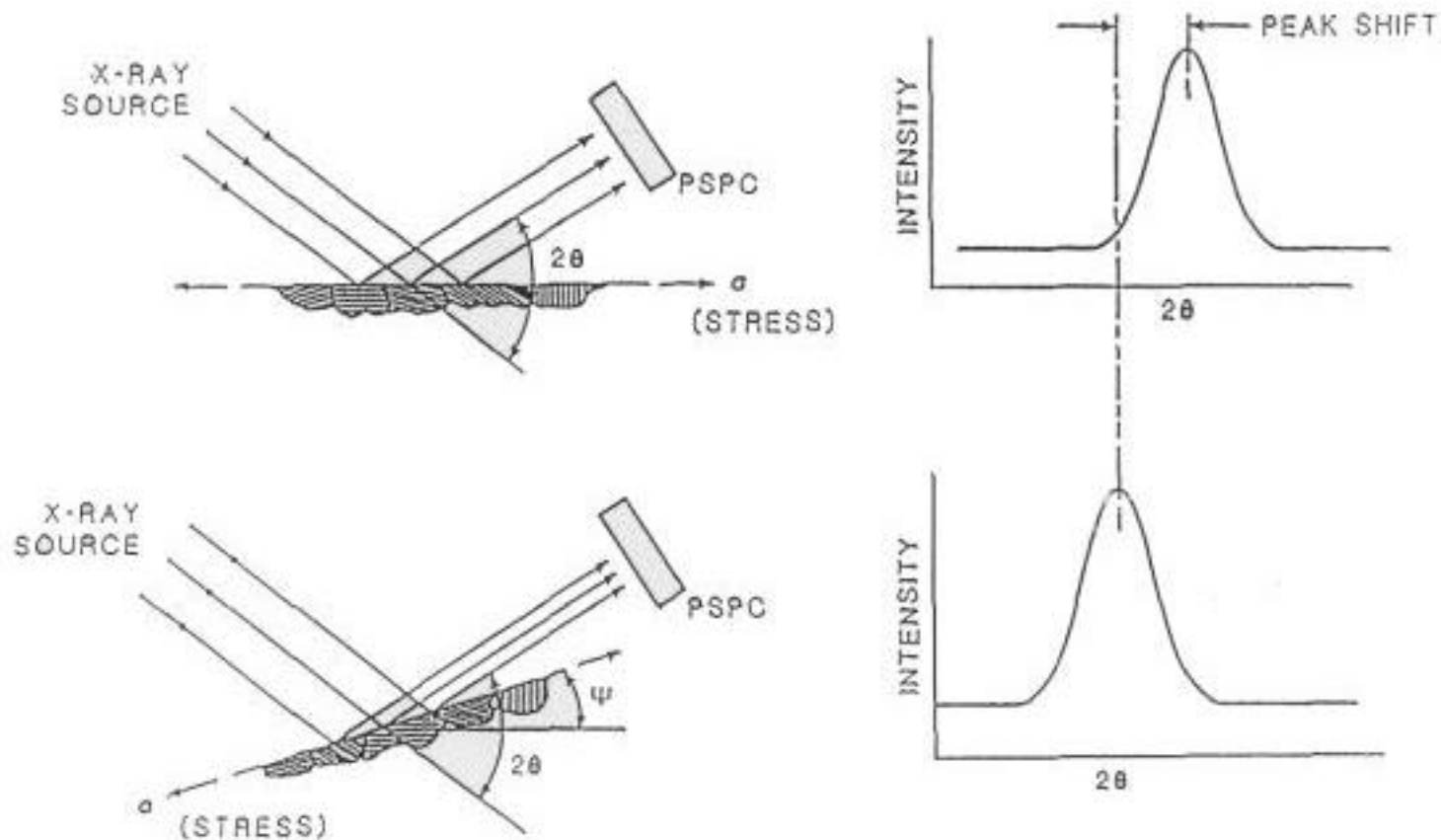
$$1/2 S_2 = \frac{1 + \nu}{E} \quad S_1 = \frac{-\nu}{E}$$



# Single Exposure Technique



# Double and Multiple Exposure Technique





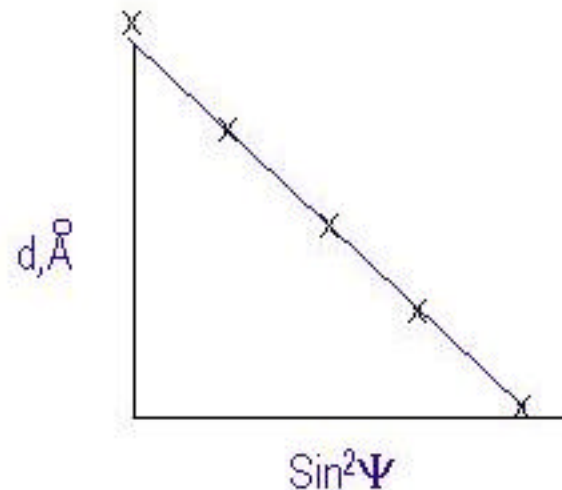
## Multiple Exposure ( $\sin^2\psi$ ) Technique

$$\sigma_{\phi} = \frac{d_{\phi\psi} - d_{\phi\psi} = 0}{1/2S_2 \sin^2\psi d_0} = \frac{m}{(1+\nu)/E d_{\phi\psi} = 0}$$


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## Multiple Exposure ( $\sin^2\psi$ ) Technique

$$\sigma_{\phi} = \frac{d_{\phi\psi} - d_{\phi\psi=0}}{1/2S_2 \sin^2\psi d_0} = \frac{m}{\frac{(1+\nu)}{E} d_{\perp}}$$



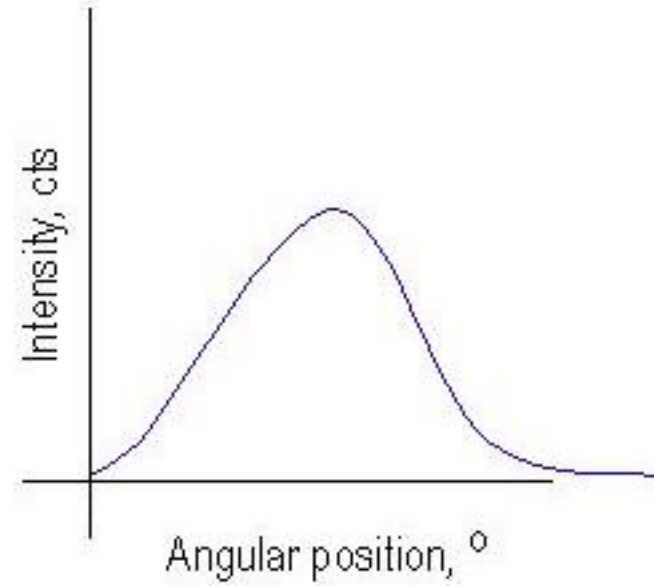
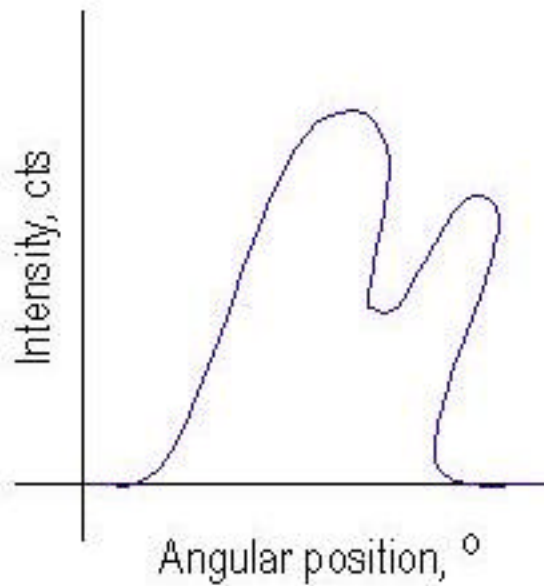
## X-Ray Diffraction Stress Measurement

- Can distinguish metallurgical and mechanical conditions such as:
    - large grain size
    - preferred orientation
    - stress gradients
    - surface distortion
    - shear stresses
    - plastic strain indication
    - hardness in steels
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## X-Ray Diffraction Stress Measurements

- Peak width analysis
    - Indication of plastic strain
    - Can be calibrated to indicate hardness in steels
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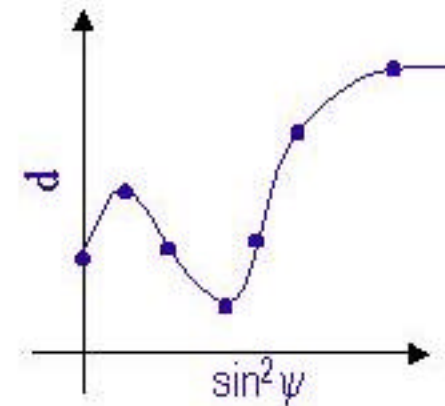
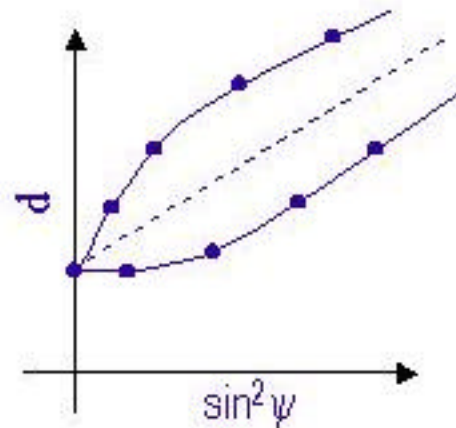
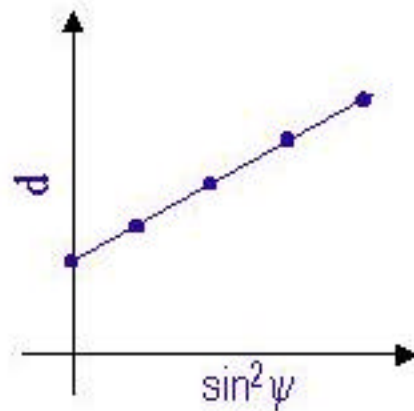
# Peak Width Analysis



## X-Ray Diffraction Stress Measurements

- Depth profiling corrections
  - Stress Gradient corrections
  - Layer removal correction

## Examples of d-spacing Versus $\sin^2\psi$ Plots



## Monitor and Control Quality of Many Processes

- Shot Peening
  - Grinding
  - Heat Treating
  - Plating
  - Welding
  - Forging
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## Aerospace Applications

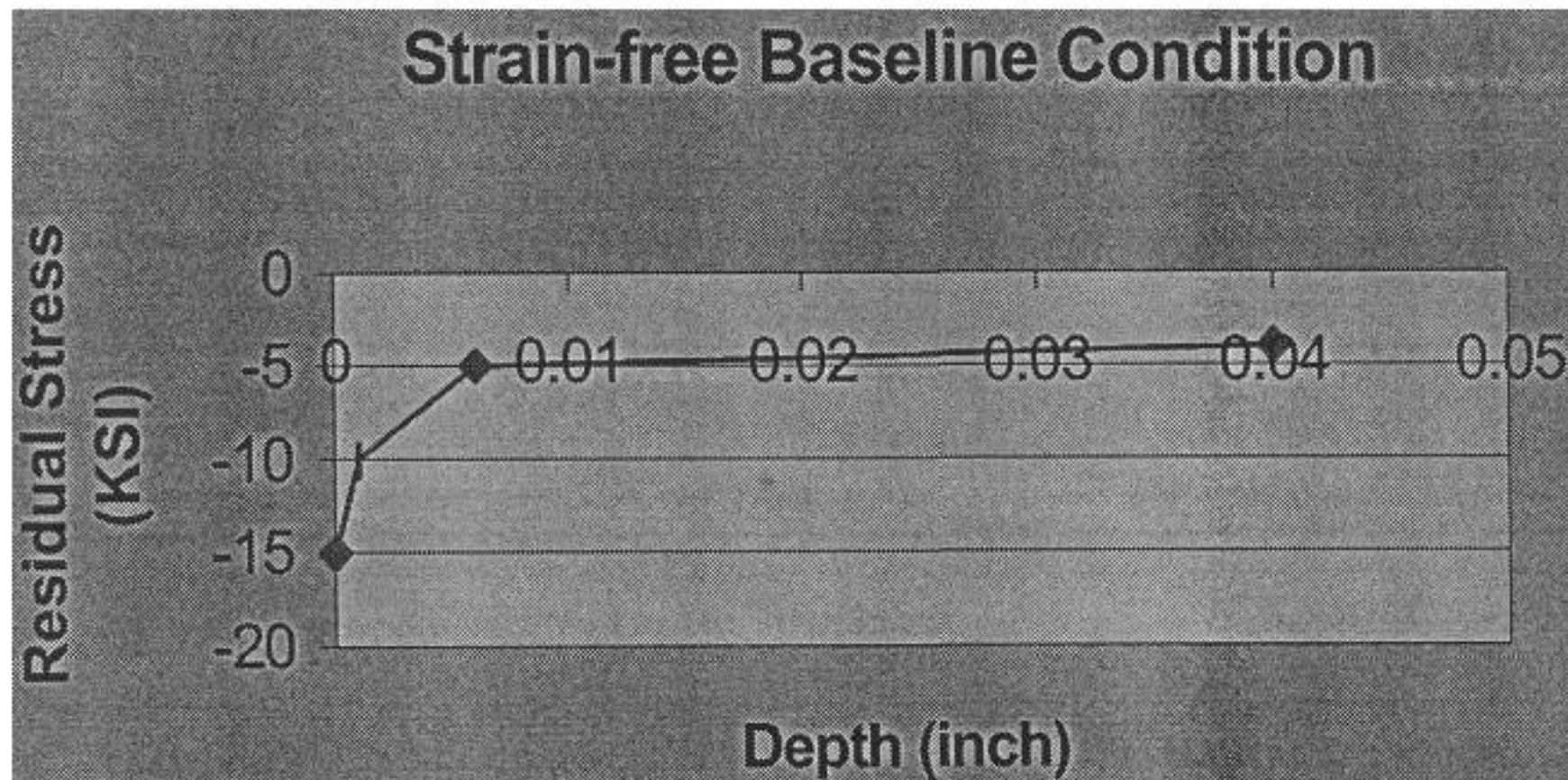
- Engine Components
    - Fan Blades, Compressor Blades, Turbine Blades, Disks, Diffusers, Bearings, Propeller Blades
  - Rocket Motor Cases
  - Structures
    - Landing Gears, Skins, Wheels, Bulkhead, Wing Spars
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## The TEC 4000 X-Ray Diffraction System



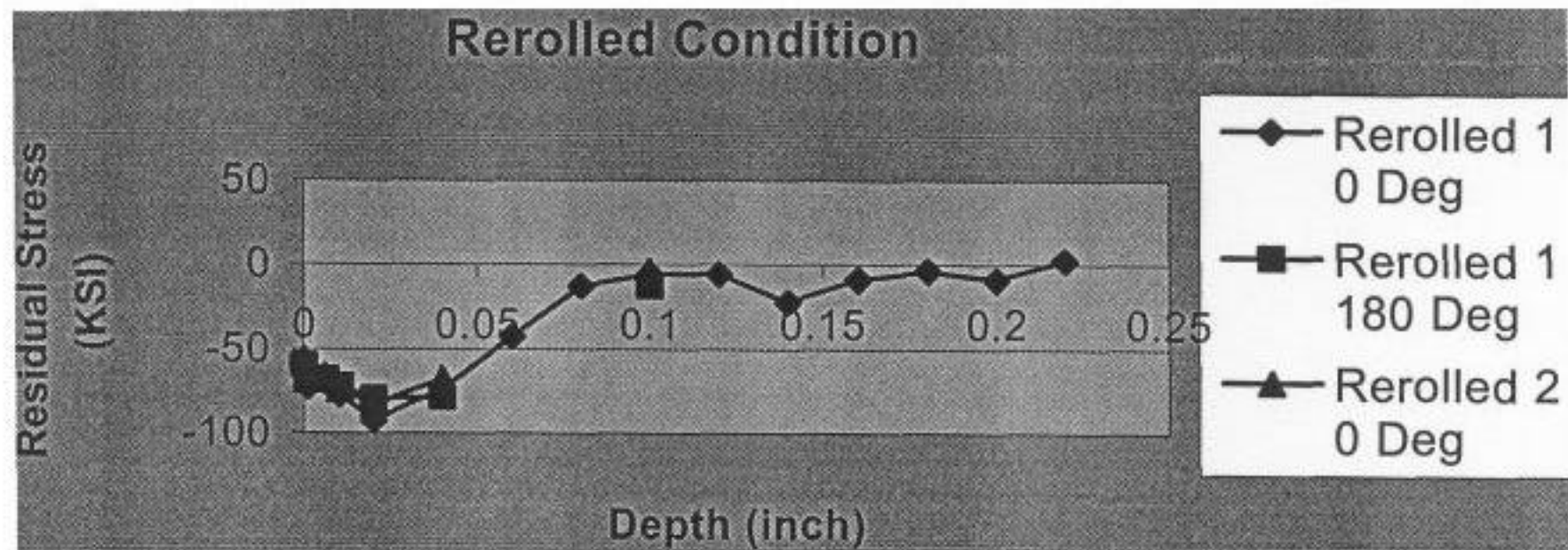
## Results

Residual stress profile in strain-free baseline propeller blade sample.



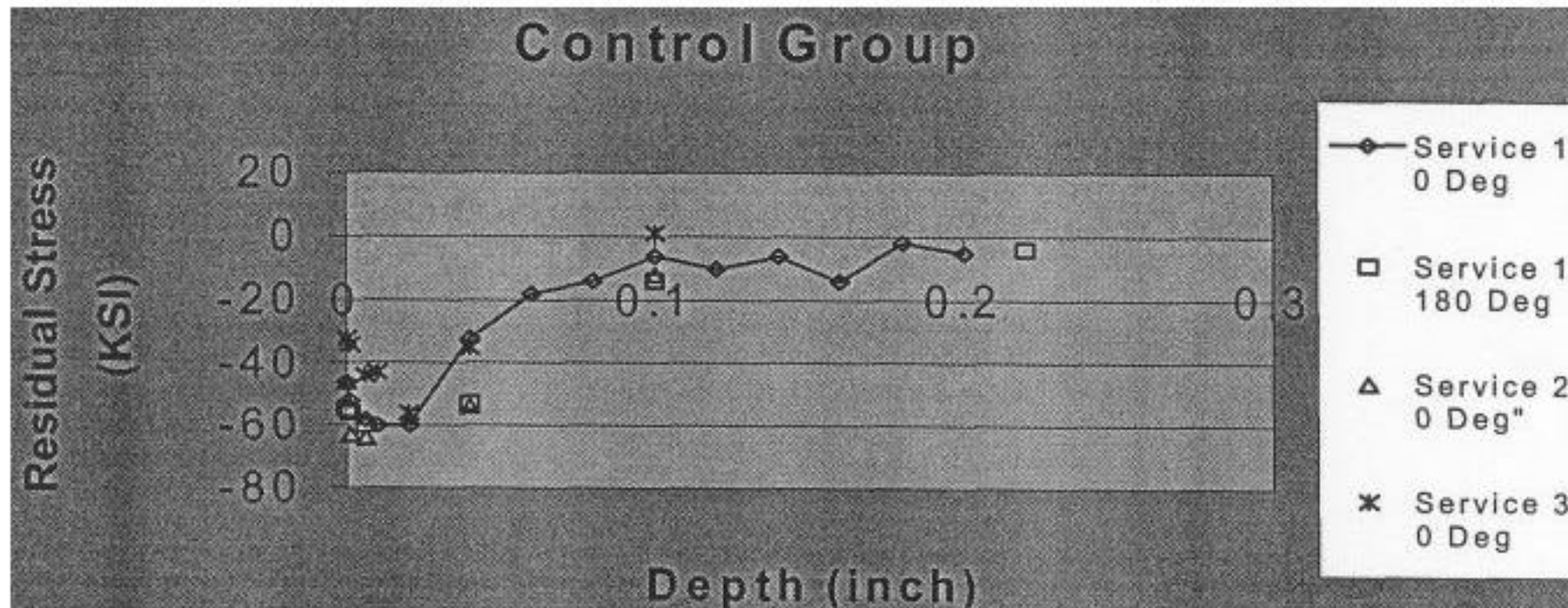
# Results

Residual stress levels after cold rolling, as measured in the shank



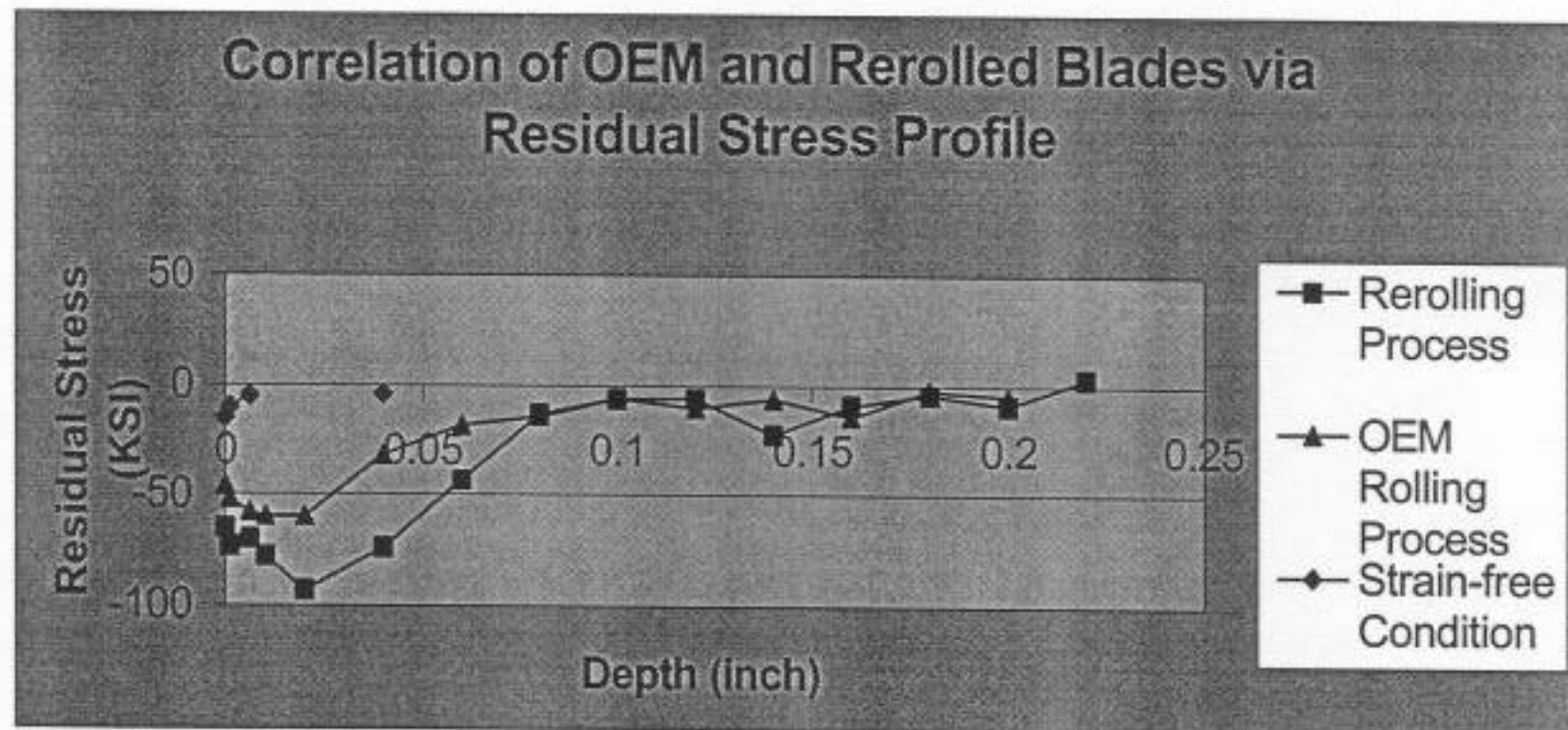
## Results

Residual stress profiles of the group of OEM-rolled service blades



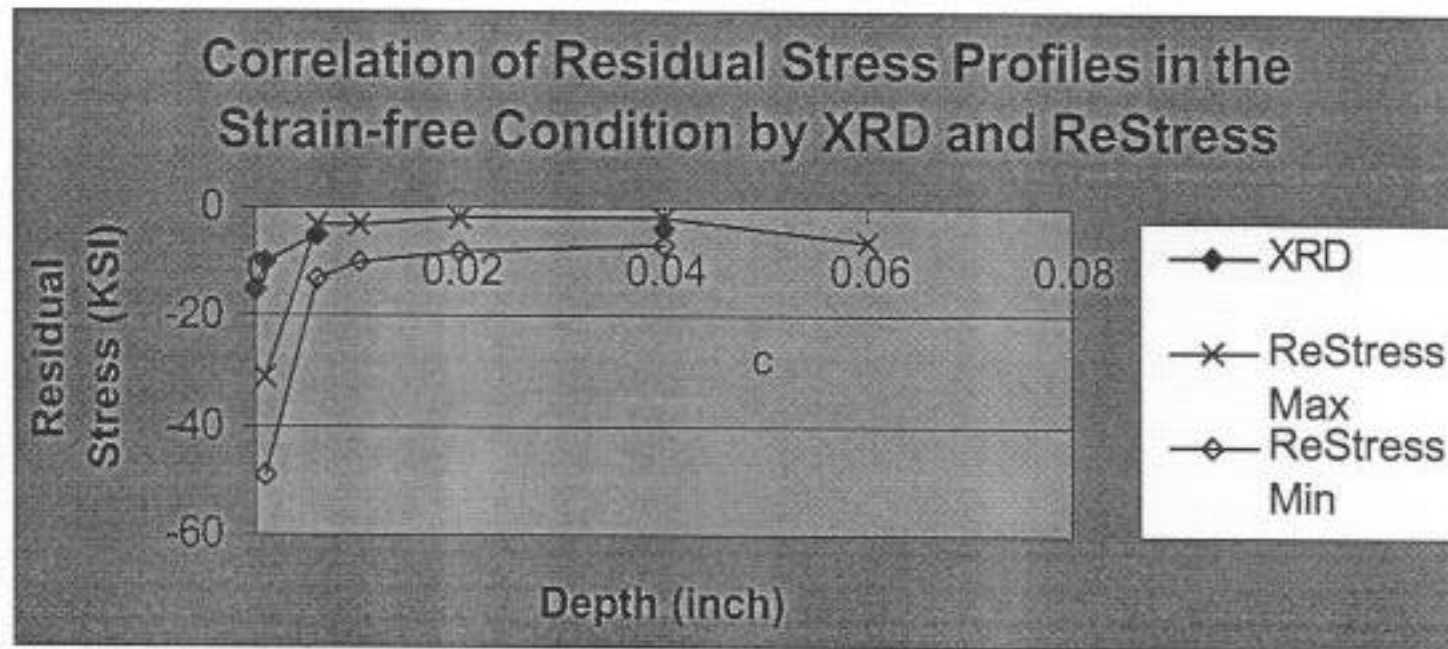
## Results

Comparison of residual stress profiles resulting from organic rerolling and OEM rolling



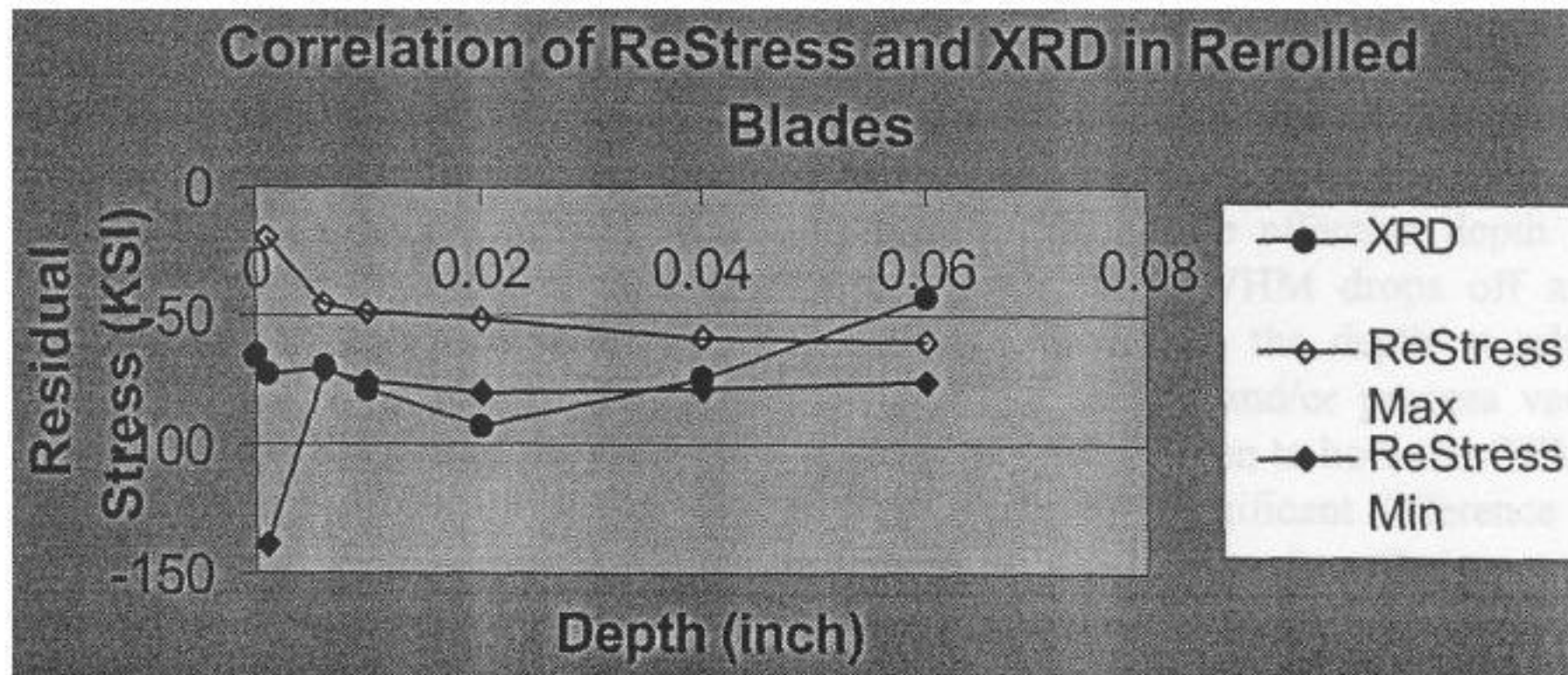
# Results

Correlation of principle residual stresses by x-ray diffraction and equivalent uniform stresses by Restress in the strain-free case



# Results

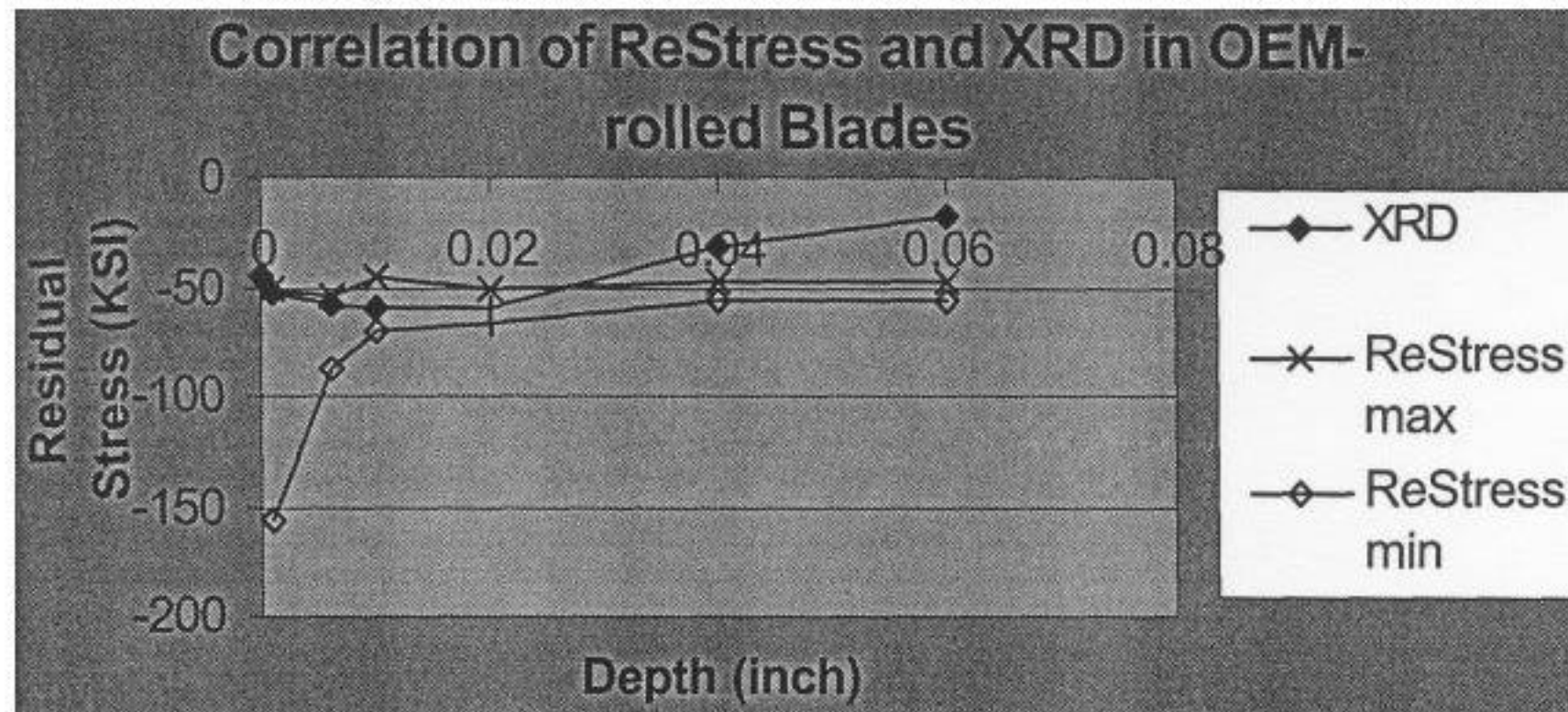
Correlation of principle residual stresses by x-ray diffraction and equivalent uniform stresses by Restress in the re-rolled case





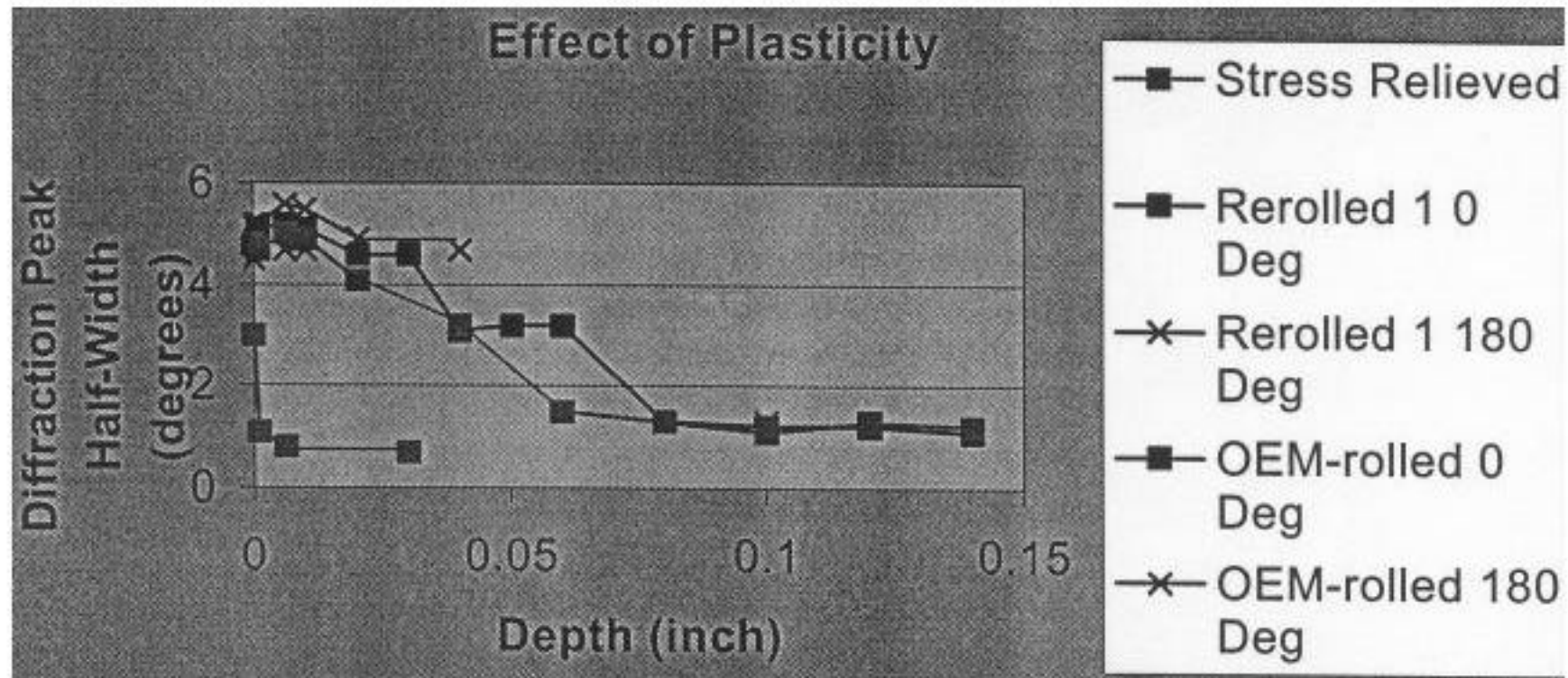
# Results

Correlation of principle residual stresses by x-ray diffraction and equivalent uniform stresses by Restress in the OEM-rolled case



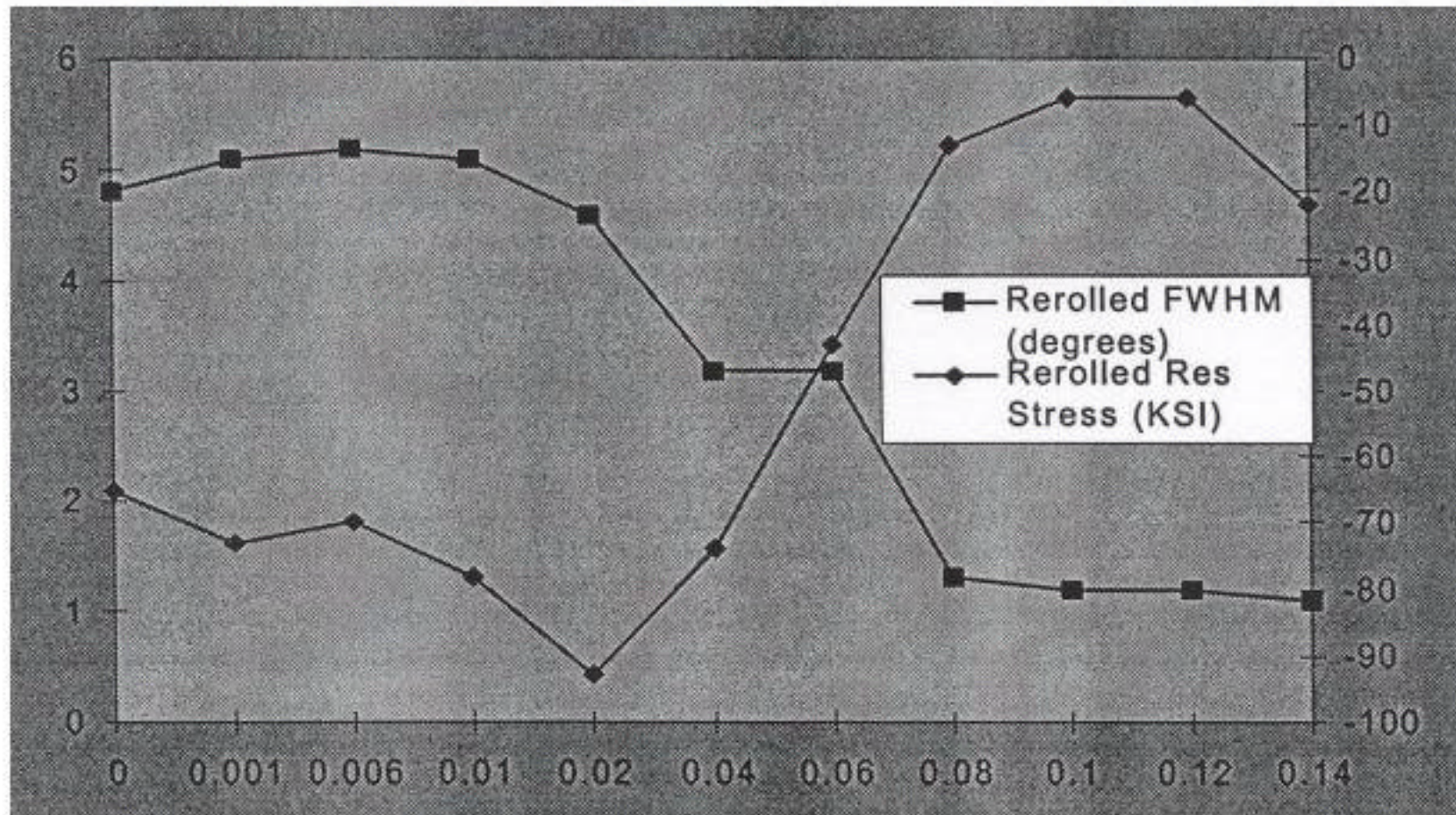
## Results

### Depth of plasticity in rerolled and OEM-rolled conditions



# Results

Correlation of Residual Stress and Diffraction Peak Width Profiles



## Conclusions

- Due to severity of service conditions, beneficial compressive stresses can be induced by rolling propellers during manufacturing
  - Blades can be rerolled to restore beneficial stresses that fade during service
  - Stress levels at and through the surface can be determined by x-ray diffraction
-